



Concepts of Programming Language Design

Featherweight Java

Overview

tools to talk about languages

higher & first-order syntax

inference rules, induction

abstract machines

big step and small step operational semantics

value & type environments

parametric polymorphism/
generics

control stacks

(algebraic) data types

sub typing

overloading

partial application/function closures

semantic features

functional

OO
inheritance/subclassing

static & dynamic
scoping

static & dynamic
typing

language concepts

procedural/imperative

explicit & implicit
typing



Object oriented languages

- What are the characteristics of an object oriented language?
 - objects bundle data and behaviour
 - ▶ the object knows what to do
 - inheritance
 - ▶ subclass relationship in the type system
 - method overloading as a form of polymorphism
 - abstraction (or encapsulation):
 - ▶ hiding implementation details from the user, interaction through restricted interface



Object oriented languages

- We will look at these language features today (apart from abstraction) using Featherweight Java, a simple object oriented language
- we only look at the features which didn't occur in other languages
 - e.g., no destructive updates, arithmetic expressions, loops,...



Featherweight Java

- Minimal OO language

prgm ::= *cdec*s *expr*
*cdec*s ::= *cdecl* *cdec*s
cdecl ::= **class** *classN* **extends** *classN* { *classN* *fieldN* ; *cons* *method* }
cons ::= *classN* (*classN* *varN*) { **super** (*varN*) ; **this.***fieldN* = *varN* ; }
method ::= *classN* *methodN* (*classN* *varN*) { **return** *e* } ;
 τ ::= *classN*
e ::= *varN* | *e.**fieldN* | *e.**methodN*(*e*) | **new** *classN* (*e*) | (*classN*) *e*

- TinyC like expressions and statements could be added to make it a proper language
 - most would not add anything of interest for our purposes
 - destructive updates would be interesting (but discussed in the context of ref types):
 - does an assignment copy the object or just the reference?



Featherweight Java

- Class expressions `class classN extends classN { classN fieldN ; cons method }`

```
class C extends C'
{
  C1 f1;
  C2 f2;
  ...
  k
  d1
  d2
  ...
}
```

declares a class

- *C* to be a subclass of *C'*
- with additional fields *C*_{*i*} *f*_{*i*}
- a single constructor *k*
- methods *d*_{*i*}



Featherweight Java

classN (*classN varN*) {super (*varN*); this.*fieldN=varN*;}

- Constructor expressions

```
C (C'1 x'1;...;C1 x1;...){  
  super (x'1,...)  
  this.f1 = x1;  
  this.f2 = x2;  
  ...  
}
```

declares a constructor for a class

- with arguments *C*'₁ *x*'₁ corresponding to a superclass
- with arguments *C*₁ *x*₁ corresponding to the new fields of the subclass
- *x*'₁ are initialised via the superclass
- **this.***f*_{*i*} = *x*_{*i*} fields initialised in the subclass



Featherweight Java

- Method expressions

classN methodN (*classN varN*) {return *e* };

```
C m ( C1 x1 , C2 x2 , ... ) {return e ;}
```

declares a method *m*

- which returns a value of class *C*
- with arguments *x_i* of class *C_i*
- and a body returning the value of expression *e*
- methods of the parent class can be overwritten (type has to stay the same)



Featherweight Java

- Field selection

$e.f$

select a field f from instance e

- Method invocation

$e.m (e_1, e_2, \dots)$

invoke a method m of instance e with arguments e_1, e_2, \dots



Featherweight Java

- Instance creation

```
new C ( e1, e2, ... )
```

creates new instance of class *C* with arguments *e*₁, *e*₂, ...

- Casting

```
( C ) e
```

casts a value *e* to class *C*

What should the semantics of a cast be?

- change the static type of the object to be *C*, but don't change the object
- this is only ok if the actual type of *e* is a subclass of *C*



Featherweight Java

- Types

- the set of types is limited to the set of class names
- in examples, we assume the presence of types like `int` and `bool`, but we will not discuss the semantics of these types

there is a class `Object`

- all other classes are subclasses of `Object`

a special variable `this` referring to the instance itself



Subclasses and Subtypes

- Subclass/superclass relationship:
 - similar to the subtype/supertype relationship, but more restrictive
 - if c is a subclass of c' , then c has at least as many fields and methods as c'
 - objects of class c can be coerced to c' by ignoring the additional fields
 - we write $c <: c'$ to denote the subclass relationship



```

class Point extends Object {
    int x;
    int y;

    Point (int x, int y) {
        super ();
        this.x = x;
        this.y = y;
    }
}

class ColourPoint extends Point {
    Colour c;

    ColourPoint (int x, int y, Colour c) {
        super (x, y);
        this.c = c;
    }

    Colour getc () {return this.c;}
}

```

```

class Colour extends Object {
    int red;
    int green;
    int blue;

    Colour (int r, int g, int b) {
        super ();
        this.red    = r % 256;
        this.green  = g % 256;
        this.blue   = b % 256;
    }
}

```



Static Semantics

- The static semantics is defined by the following judgements:

| | |
|---|-------------------------|
| $c <: c$ | subclass relationship |
| $\Gamma \vdash e : c$ | expression typing |
| $m \text{ ok in } c$ | well formed method |
| $c \text{ ok}$ | well formed class |
| $T \text{ ok}$ | well formed class table |
| $\text{fields } (c) = \{c_1 f_1, c_2 f_2, \dots\}$ | field lookup |
| $\text{type } (m, c) = \underline{c} \rightarrow c$ | method type |

- A program consists of a class table T (sequence of class declarations) and an expression e .
- We use the class table T as implicit parameter in the following.
- We only look at some interesting aspects of the static semantics.



Static Semantics

- Similar to other languages, we need to check:
 - are variable names in scope?
 - are methods called with the correct arguments?
 - if fields are accessed, are the fields attributes of the class?
 - we need to keep track of the type (ie, class) of an expression
- What is new?
 - the static type and the dynamic type are not necessarily the same!



- Fields

- we define a judgement to determine the field names and the types of a given class:

$$\textit{fields}(\textit{className}) = \{ \textit{className}_1 \textit{fieldName}_1, \dots \}$$

$$\overline{\textit{fields}(\texttt{Object}) = \bullet}$$

$$\frac{T(c) = \texttt{class } c \texttt{ extends } c' \{ \underline{c} \textit{f}; \dots \} \quad \textit{fields}(c') = \underline{c'} \textit{f'}}{\textit{fields}(c) = \underline{c'} \textit{f'}, \underline{c} \textit{f}}$$



Static semantics

- Typing judgment for expressions of the language

$$\Gamma \vdash e : c$$

- Every variable has to be declared

$$\frac{x : c \in \Gamma}{\Gamma \vdash x : c}$$

$$\frac{\Gamma \vdash e_0 : c_0 \quad \textit{fields}(c_0) = c_1 \ f_1 \ \dots}{\Gamma \vdash e_0 . f_i : c_i}$$



Static Semantics

- Method invocation

- argument and result types of methods are stored in the class table
- we need to define a function *type*, which, given a method and class, returns the type of that method (we'll leave that for later)
- methods of super types can be applied without cast

$$\begin{array}{c} e_1 : c_1, e_2 : c_2, \dots \qquad c_1 <: c'_1, c_2 <: c'_2, \dots \\ \text{ } \qquad \qquad \qquad \nearrow \qquad \qquad \qquad \nearrow \\ \hline \Gamma \vdash e_0 : c_0 \quad \Gamma \vdash \underline{e} : \underline{c} \quad \text{type}(m, c_0) = \underline{c}' \rightarrow c_1 \quad \underline{c} <: \underline{c}' \\ \hline \Gamma \vdash e_0.m(\underline{e}) : c_1 \end{array}$$

- Instantiation

$$\frac{\Gamma \vdash \underline{e} : \underline{c} \quad \underline{c} <: \underline{c}' \quad \text{fields}(c) = \underline{c}' f}{\Gamma \vdash \text{new } c(\underline{e}) : c}$$



Static Semantics

- All casts are *statically* valid

$$\frac{\Gamma \vdash e_0 : c'}{\Gamma \vdash (c)e_0 : c}$$



- Subclass relationship

$$\overline{c <: c}$$

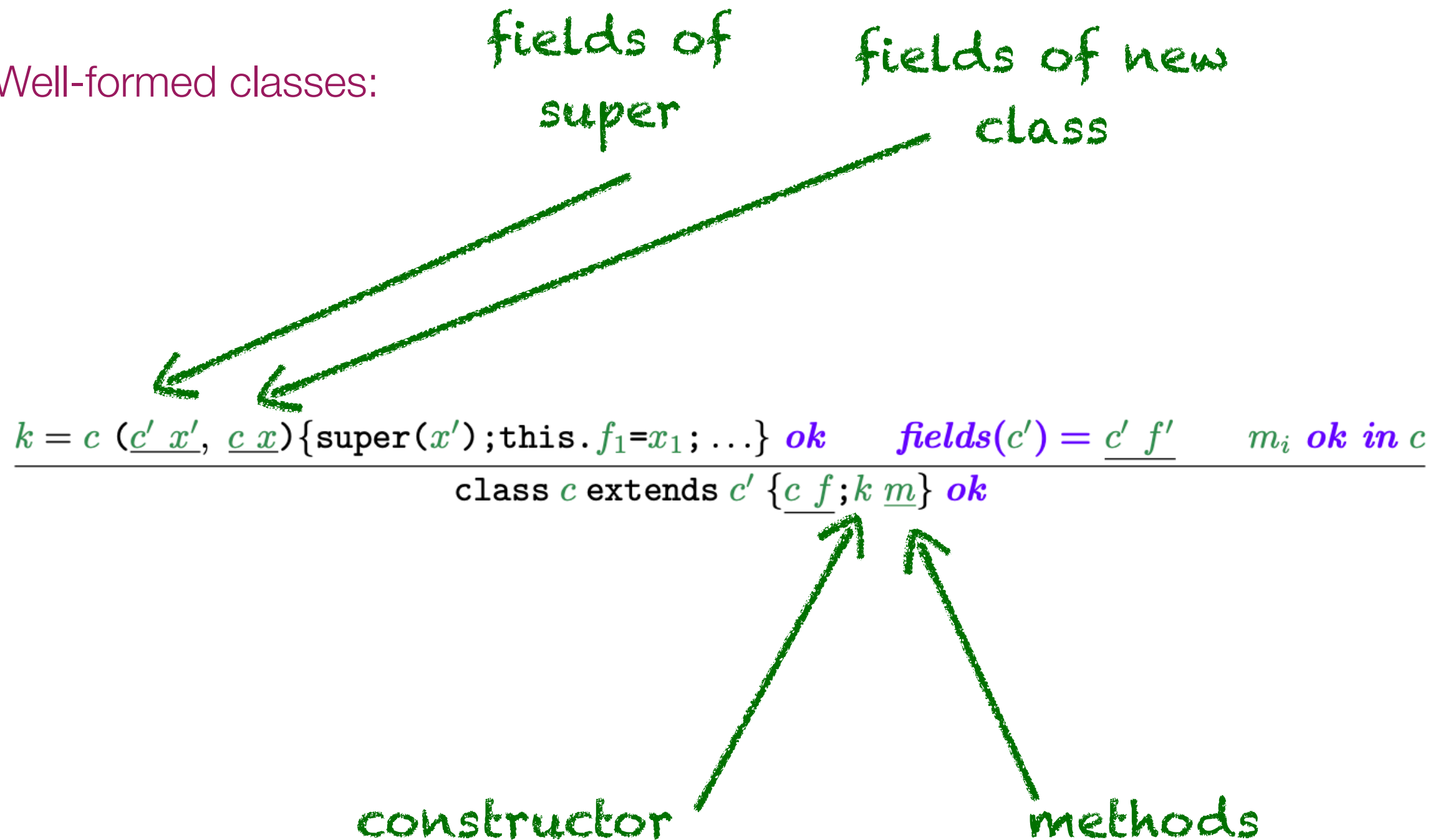
$$\frac{c <: c' \quad c' <: c''}{c <: c''}$$

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots \}}{c <: c'}$$



Static Semantics

- Well-formed classes:



Static Semantics

$$\frac{k = c(\underline{c'} \ x', \underline{c} \ x) \{ \text{super}(x'); \text{this}.f_1 = x_1; \dots \} \text{ ok} \quad \text{fields}(c') = \underline{c'} \ f' \quad m_i \text{ ok in } c}{\text{class } c \text{ extends } c' \{ \underline{c} \ f; k \ \underline{m} \} \text{ ok}}$$

```

      C          C'
class ColourPoint extends Point {
  Colour c; C f
  k ColourPoint (int x, int y, Colour c) {
    super (x, y);
    this.c = c;
  }
  m Colour getc () {return this.c;}
}
    
```



Static Semantics

To find the type of a method m of a class c , we have to search upwards in the class hierarchy for the definition of m .

methods defined in this class

the method we're looking for

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots; \dots \underline{m''} \} \quad m''_i = c_i \ m(\underline{c_i} \ x_i) \{ \text{return } e \}}{type(m, c) = \underline{c_i} \rightarrow c_i}$$

the method we're looking for is not defined in this class

so check parent class

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots; \dots \underline{m''} \} \quad m \notin m'' \quad type(m, c') = \underline{c_i} \rightarrow c_i}{type(m, c) = \underline{c_i} \rightarrow c_i}$$

$$\frac{}{type(m, \text{Object}) = \text{noType}}$$



Static Semantics

- **Method overriding:** new subclass methods must have

- the same argument type
- the same result type

as the superclass method

then just make sure the body of the method is well typed

the method not present in any of the parent classes

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots \} \quad \text{type}(m, c') = \text{noType} \quad \underline{x:c}; \text{this} : c \vdash e_0 : c_0}{c_0 \ m(\underline{c} \ x) \{ \text{return } e_0 \}; \text{ok in } c}$$

the method present in one of the parent classes

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots \} \quad \text{type}(m, c') = \underline{c} \rightarrow c_0 \quad \underline{x:c}; \text{this} : c \vdash e_0 : c_0}{c_0 \ m(\underline{c} \ x) \{ \text{return } e_0 \}; \text{ok in } c}$$

make sure method has the same type as in parent class



- Properties

- casts may fail at run time: checks required
- method invocation is statically checked
- field selection is statically checked
- objects have a statically determined type, but their actual type at runtime might be different
 - ▶ static vs actual dynamic type
 - ▶ dynamic semantics has to take it into account to preserve type safety!



Dynamic Semantics

- We discuss parts of the single step or structural operational semantics of Featherweight Java
- **Values:** an instance is a value if all of it's arguments are values

$$\frac{\underline{v} \text{ value}}{\text{new } c(\underline{v}) \text{ value}}$$

in essence, an instance is just a collection of named fields, labelled with class names

- If not all the arguments of a constructor (or method invocation) are evaluated yet, we evaluate from the left to the right (no side effects, so order doesn't actually matter)

$$\frac{e \mapsto e'}{\text{new } c(\underline{v}, e, \underline{e}) \mapsto \text{new } c(\underline{v}, e', \underline{e})}$$



Dynamic Semantics

- Field Selection

- $c_i' f_i'$: fields of a superclass
- $c_i f_i$: fields of a class itself
- retrieve values of field from either superclass or class itself

$$\frac{\textit{fields}(c) = \underline{c'} \underline{f'}; \underline{c} \underline{f};}{\text{new } c(\underline{v'}, \underline{v}).\underline{f'_i} \mapsto \underline{v'_i}}$$



Dynamic Semantics

- Field Selection

- $c_i' f_i'$: fields of a superclass
- $c_i f_i$: fields of a class itself
- retrieve values of field from either superclass or class itself

$$\frac{\text{fields}(c) = \underline{c'} f'; \underline{c} f;}{\text{new } c(\underline{v'}, \underline{v}).f'_i \mapsto v'_i}$$

$$\frac{\text{fields}(c) = \underline{c'} f'; \underline{c} f;}{\text{new } c(\underline{v'}, \underline{v}).f_j \mapsto v_j}$$

Note: contents of fields cannot be changed after initialisation.

We could extend the language using the techniques described previously



Dynamic Semantics

- Type Cast $(c')\mathbf{new}\ c(\underline{v})$
 - if c' is a super type of c , the cast is just ignored
 - otherwise, cause a checked run-time error

$$\frac{c <: c'}{(c')\mathbf{new}\ c(\underline{v}) \mapsto \mathbf{new}\ c(\underline{v})}$$

$$\frac{c' \not<: c}{(c')\mathbf{new}\ c(\underline{v}) \mapsto \mathbf{error}}$$

➡ during evaluation, we discard the information about the static type!



Dynamic Semantics

- Method Invocation

- how can we find the correct methods for method invocation?

`new c (v) . m(v')` \mapsto ?



- Dynamic Dispatch

- find the body of a method m of a class c , we search upwards in the class hierarchy for the first definition of m .

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots \underline{m} \} \quad m_i = c_i \quad m(\underline{c}_i \underline{x}) \{ \text{return}(e) \}}{\text{body}(m, c) = \underline{x} \rightarrow e}$$



- Dynamic Dispatch

- find the body of a method m of a class c , we search upwards in the class hierarchy for the first definition of m .

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots \underline{m} \} \quad m_i = c_i \quad m(\underline{c}_i \underline{x}) \{ \text{return}(e) \}}{\text{body}(m, c) = \underline{x} \rightarrow e}$$

$$\frac{T(c) = \text{class } c \text{ extends } c' \{ \dots \underline{m} \} \quad m \notin \underline{m} \quad \text{body}(m, c') = \underline{x} \rightarrow e}{\text{body}(m, c) = \underline{x} \rightarrow e}$$



Dynamic Semantics

- Method Invocation

- method invocation relies on an auxiliary predicate, *body* (defined later) which provides the list of formal arguments and the body of a method *m* defined in a class *c*
- replace all formal parameters *x* by actual parameters *v'*
- replace every occurrence of **this** by the instance itself
- substitution semantics is possible, because we have no destructive updates in the language

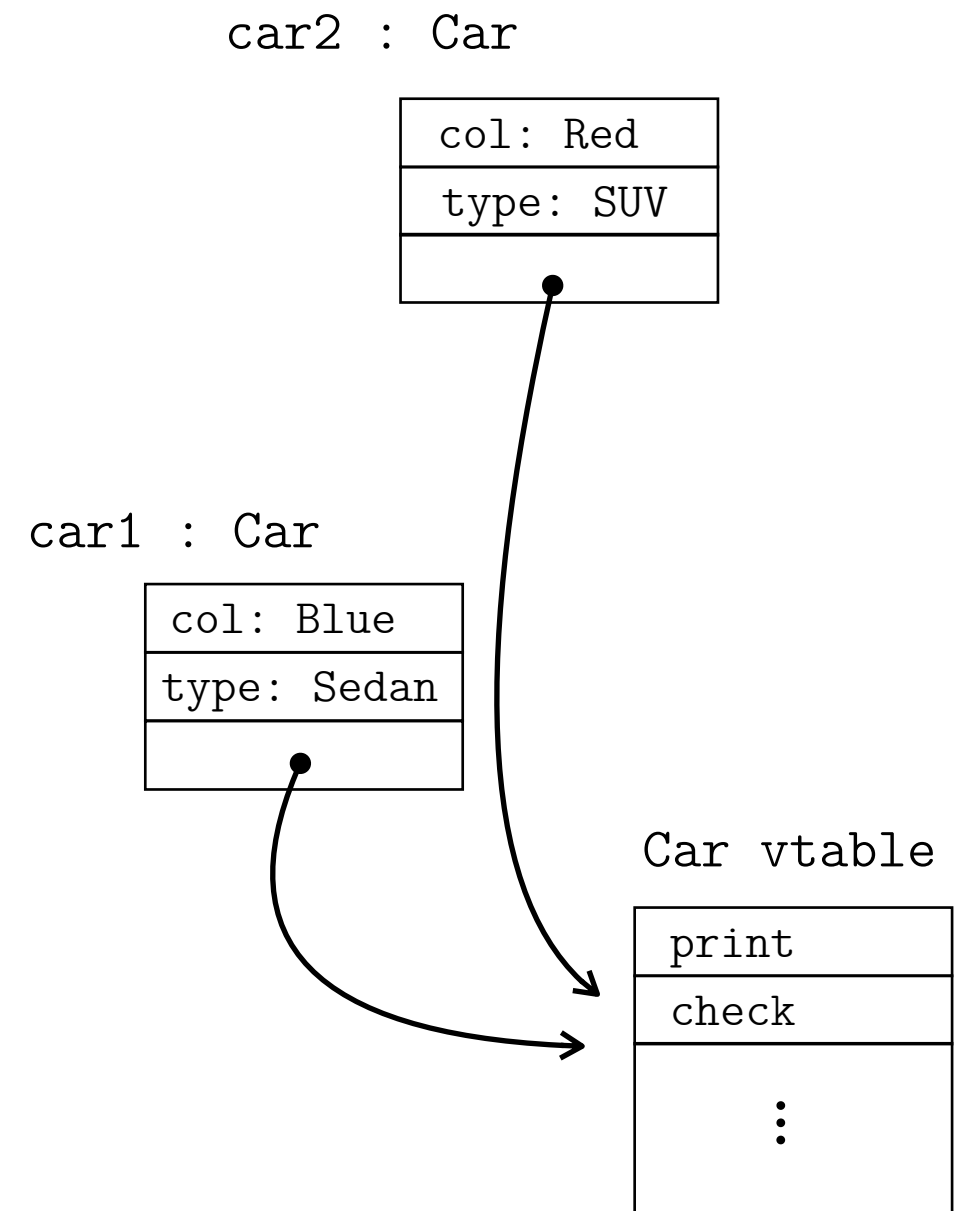
$$\frac{\textit{body}(m, c) = \underline{x} \rightarrow e_0}{\text{new } c(\underline{v}) . m(\underline{v}') \mapsto e_0[\underline{x} := \underline{v}'][\text{this} := \text{new } c(\underline{v})]}$$



Dynamic Semantics

- How is method invocation implemented?

- searching for the method every time would be too slow!
- objects have a hidden field
 - ▶ reference to a (virtual) method table, which contains references to all methods of the class
 - ▶ table shared among all the objects of a class
 - ▶ not necessary to traverse the whole class hierarchy at runtime, because table for a class can be determined at compile time
 - ▶ still, it's more expensive than a regular function call



Type Safety

- Is Featherweight Java type safe?

- dynamic semantics of casts preserves actual (ie, dynamic) type of an instance
- the actual type of an expression may be “smaller” in the subtype ordering during execution

- Preservation:

If $e:c$ and $e \mapsto e'$, then $e':c'$ for some c' such that $c' \leq c$

- Progress

If $e:c$ then either

1. e is a value $\text{new } c'(\underline{v})$, with $c' \leq c$ or
2. e is equal to $(c)\text{new } c'(\underline{v})$, with $c' \not\leq c$, then $e \mapsto \text{error}$ or
3. there exists e' , such that $e \mapsto e'$



Conditionals and subtyping

- What should the type of a conditional expression be?

`if e then e1 else e2`



- In Featherweight Java, the subclass relationship (inheritance) is a special form of subtyping (we can coerce by ‘deleting’ fields)
- Inheritance (subclassing) and sub typing are not the same
 - inheritance is a method of code re-use through extension
 - subtyping expresses a behavioural relationship
- In Java
 - inheritance gives rise to a subtype relationship
 - not every subtype relationship in Java arises through inheritance



Java

- Featherweight Java has two types of polymorphism
- operations work on a class and all of its subclasses (form of **subtyping**)
 - methods can be **overwritten**
 - ▶ all methods have the same type, object 'knows' what the correct method is
 - dynamic dispatch default for Java, but not in C# (need to use virtual m.)
 - ▶ different to overloading, which can be resolved via type (compile time)
 - many OO language allow overloading of methods with different types
 - Haskell overloading resolved via type

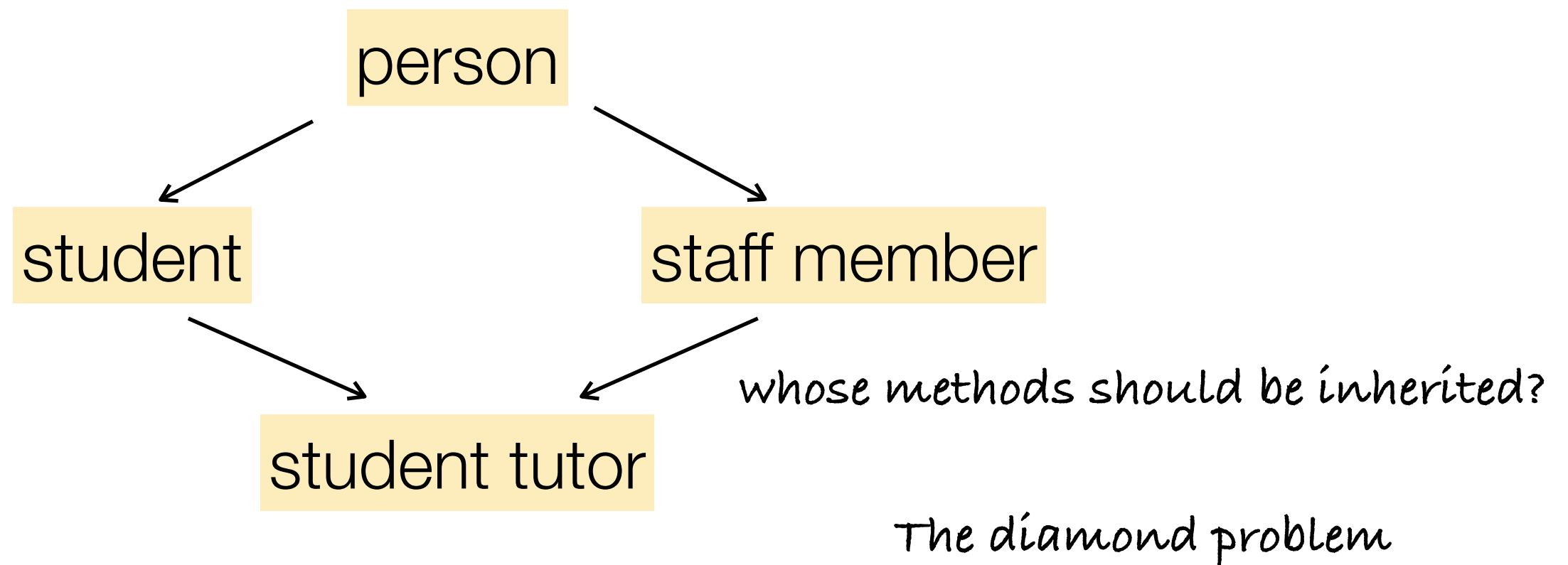
```
(==) :: Eq a => a -> a -> Bool
```

```
“123” == “Hi”
```



Multiple inheritance

- Some OO language allow classes to extend/inherit from multiple superclasses



- supported in C++, Eiffel, Python, OCaml
- not supported in C#, Swift, Java (though some features available through interfaces/interfaces)

